



Τυπολόγιο 1^{ης} Προόδου Αντοχής Υλικών II

$$n_B = \frac{\sigma_B}{\sigma_{\max}}, \quad n_F = \frac{\sigma_F / 2}{\tau_{\max}}$$

$$\sigma_{1,2} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + (\tau_{xy})^2}$$

$$\tau_{\max} = \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + (\tau_{xy})^2}$$

$$\sigma_x(y, z) = \frac{M_y}{I_y} z - \frac{M_z}{I_z} y \quad \varepsilon_x(y, z) = \frac{M_y}{EI_y} z - \frac{M_z}{EI_z} y$$

$$z = \frac{M_z}{M_y} \frac{I_y}{I_z} y + \frac{I_y}{M_y} \sigma_x$$

$$v''(x) = \frac{M(x)}{EI}$$

$$\theta(x) = v'(x)$$

$$\Delta\theta_{2-1} = F_{2-1}$$

$$\Delta v_{2-1} = F_{2-1} x_s$$

$$\frac{\partial U}{\partial P_i} = v_i, \quad \frac{\partial U}{\partial M_i} = \theta_i, \quad v_i = \int_0^L \frac{M}{EI} \frac{\partial M}{\partial P_i} dx, \quad \theta_i = \int_0^L \frac{M}{EI} \frac{\partial M}{\partial M_i} dx$$

$$U = \frac{1}{2EI} \int_0^L M_z^2(x) dx$$

$$\tau_{xy}(y) b(y) = -\frac{Q_y(x)}{I_z(x)} S_z(y) \quad S_z(y) = \int_y^{y_i} \eta dF$$

$$\tau_{xy}(y) = -\frac{3}{2} \frac{Q}{F} \left(1 - 4 \frac{y^2}{h^2}\right) \text{ (ορθογώνια διατομή, } h: \text{ διάσταση}$$

στον y-άξονα)

$$\tau_{xy}(y) = -\frac{4}{3} \frac{Q}{\pi a^4} (a^2 - y^2) \text{ (κυκλική διατομή, } a: \text{ ακτίνα}$$

κύκλου)

Διατομή I:

$$\tau_{xz}(\eta) = \frac{Q}{I_z t} \eta t \left(\frac{\eta}{2} - \frac{t}{2}\right)$$

$$\tau_{xy}(y) = \frac{Q}{I_z d} S_z(y)$$

$$\text{όπου } S_z(y) = bt \left(\frac{h}{2} - \frac{t}{2}\right) + \left(\frac{h}{2} - t - y\right) \frac{1}{2} \left(\frac{h}{2} - t + y\right) d$$

Διατομές: